

# UPPAAL SMC Tutorial: Schedulability of Herschel/Planck

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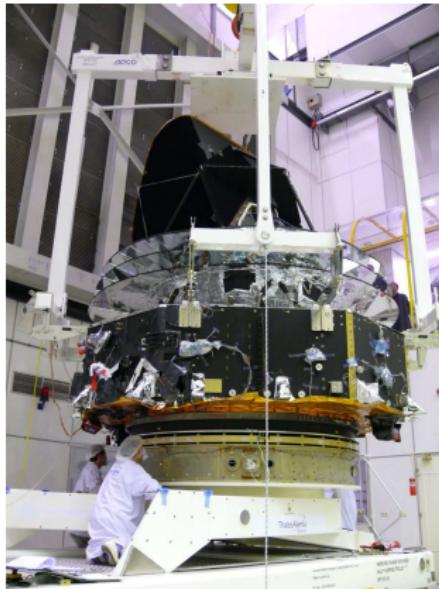
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# Outline

- 1 Satelite Mission and the Software Subsystem
- 2 Modeling
- 3 Symbolic Analysis
- 4 Statistical Analysis
- 5 Summary

# Herschel-Planck Scientific Mission at ESA



- Attitude and Orbit Control System software.
- Terma A/S: Steen Ulrik Palm, Jan Storbank Pedersen, Poul Hougaard.

# Satellite Architecture

ASW	Application software performs attitude and orbit control, handles tele-commands, fault detection isolation and recovery.
BSW	Basic software is responsible for low level communication and scheduling periodic events.
RTEMS	Real-time operating system, fixed priority preemptive scheduler.
Hardware	Single processor, a few communication buses, sensors and actuators.

# Problem Statement

- Single CPU, fixed priority preemptive scheduler.
- Mixture of 32 tasks: periodic, sporadic with dependencies.
- Mixed resource sharing (make priorities dynamic):
  - BSW tasks use priority *inheritance* protocol.
  - ASW tasks use priority *ceiling* protocol.

At Terma A/S:

- 1 out of 4 configurations *could not be proved schedulable* using schedulability analysis by Alan Burns.
- Neither simulation nor execution show any problems.

At Aalborg:

- The techniques are conservative at assuming worst case.
- *Hypothesis: model more details and achieve more accurate analysis using symbolic reachability and simulations.*

# Approach: combination of Symbolic and Statistical

Symbolic analysis:

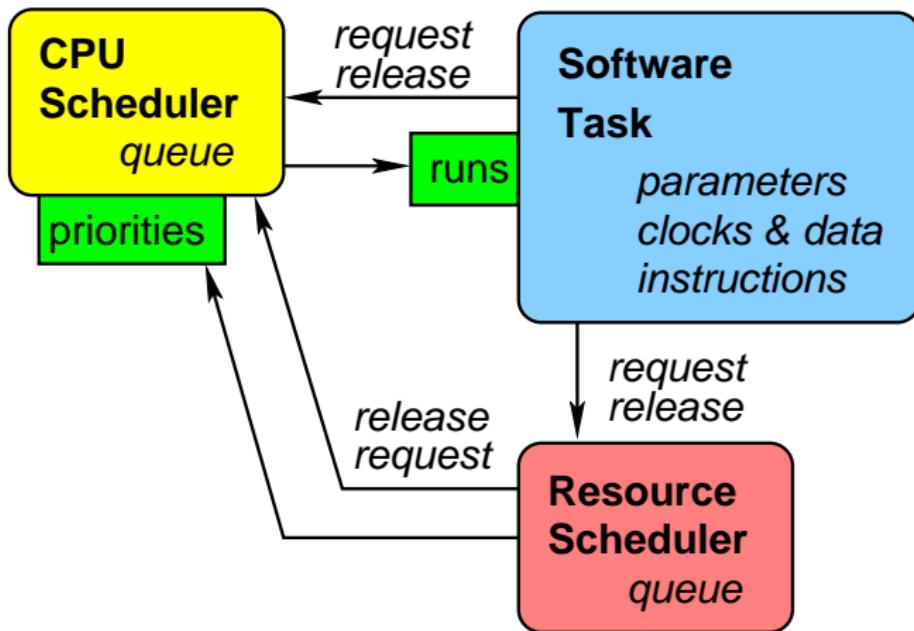
- Preemptive scheduler requires *stop-watches*.
- Exact reachability of stop-watch automata is *undecidable*.
- UPPAAL provides *over-approximation* for stop-watches.
- ⇒ symbolic analysis may give spurious errors, but still suitable for *proving safety/schedulability*.

Statistical analysis:

- can show *presence of errors* but not absence.
- ⇒ suitable for *disproving schedulability*.

$f = \text{BCET}/\text{WCET}$ :	0-71%	72-86%	87-89%	90-100%
Symbolic MC:	maybe	maybe	n/a	<b>Safe</b>
Statistical MC:	<b>Unsafe</b>	maybe	maybe	maybe

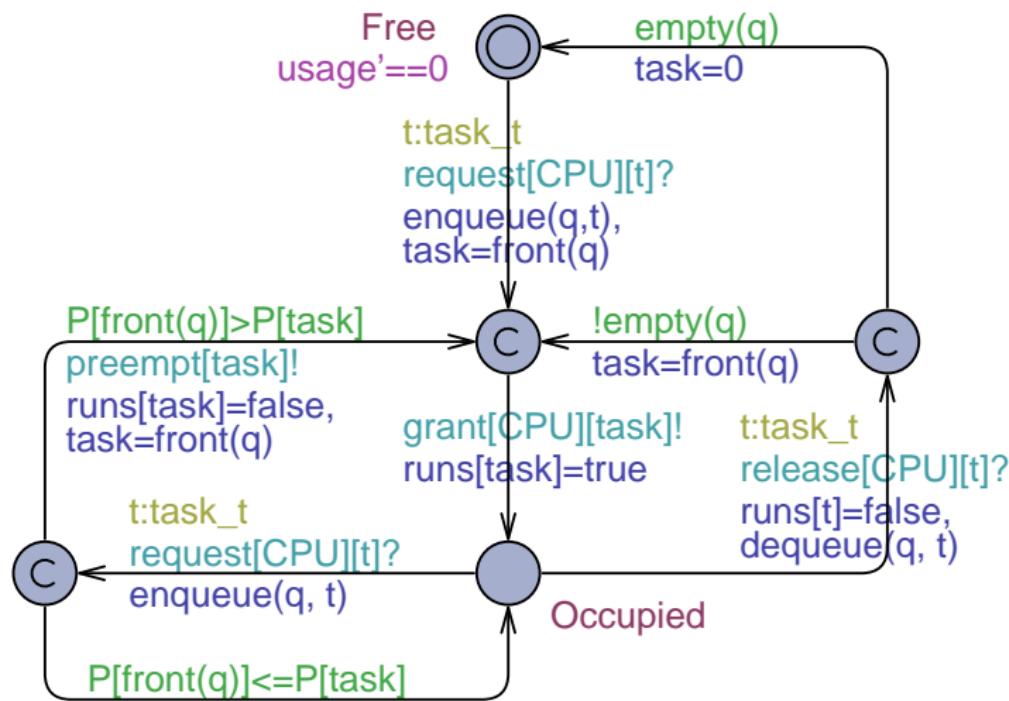
# Model Overview



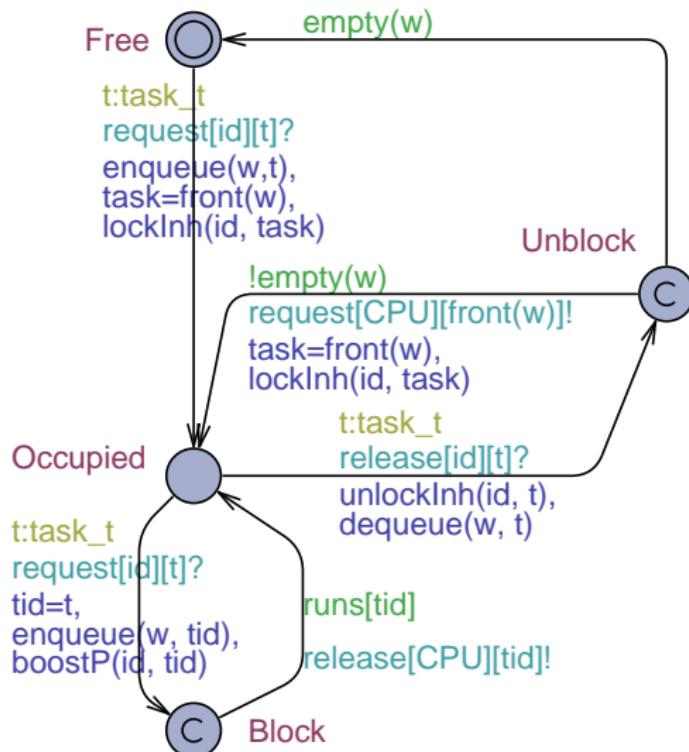
# Some Declarations

```
1  const int NRTASK = 3; // number of tasks
2  typedef int [1, NRTASK] task_t; // type for task identifier
3  int P[task_t] = { 3, 2, 1 }; // task priorities as ints
4  task_t task; // currently executed task
5
6  const int NRRES = 1; // number of resources
7  typedef int [1, NRRES] res_t; // type for resource id
8  tasks_t owner[res_t]; // current resource owner
9
10 clock usage; // CPU usage
11
12 typedef tasks_t list_t [NRTASK]; // list of tasks
13 typedef struct {
14     list_t list; // list of tasks
15     int [0, NRTASK] len; // length of the list
16 } queue_t; // queue structure
```

# Fixed Priority Preemptive CPU Scheduler



# Resource Scheduler using Priority Inheritance



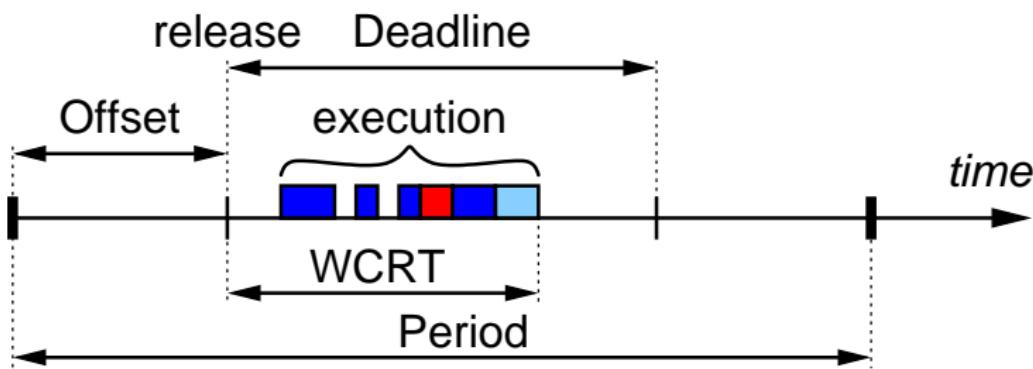
# Priority Inheritance Protocol

```
1  /** Lock/acquire: */
2  void lockInh(resid_t res, taskid_t task) {
3      owner[res] = task; // mark as occupied by the task
4  }
5  /** Unlock/release: */
6  void unlockInh(resid_t res, taskid_t task) {
7      owner[res] = 0; // mark the resource as released
8      P[task] = def_prio(task); // return to default priority
9  }
10 /** Boost the priority of resource owner: */
11 void boostPrio(resid_t res, taskid_t task) {
12     if (P[owner[res]] <= def_prio(task)) {
13         P[owner[res]] = def_prio(task)+1;
14         sort(taskqueue);
15     }
16 }
```

# Priority Ceiling Protocol

```
1  /** Lock/acquire: */
2  void lockCeil(resid_t res, taskid_t task) {
3      owner[res] = task; // mark resource occupied by the task
4      P[task] = ceiling [res]; // assume priority of resource
5  }
6  /** Unlock/release: */
7  void unlockCeil(resid_t res, taskid_t task){
8      owner[res] = 0; // mark the resource as released
9      P[task] = def_prio(task); // return to default priority
10 }
```

# Software Task Parameters



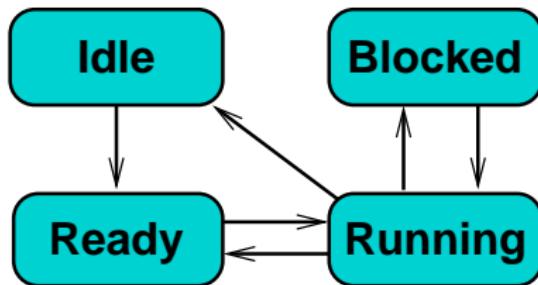
```
1 // parameter           Task1 Task2 Task3
2 const int Period[task_t] = { 100, 100, 100 };
3 const int Offset[task_t] = { 20,   0,   10  };
4 const int WCET[task_t]  = { 15,  25,  40  };
5 const int BCET[task_t]  = { 12,  20,  32  };
6 const int Deadline[task_t] = { 20,  40,  70  };
```

# Template for Task using 1 Resource

Parameters:

```
1 int Period[task_t] = { 100, 100, 100 };
2 int Offset[task_t] = { 20, 0, 10 };
3 int WCET[task_t] = { 15, 25, 40 };
4 int BCET[task_t] = { 12, 20, 32 };
5 int Deadline[task_t] = { 20, 40, 70 };
6 res_t R[task_t] = { 1, 1, 1 };
7 bool runs[task_t] = { 0, 0, 0 };
8 bool error = false; // global variable
```

OS task states:



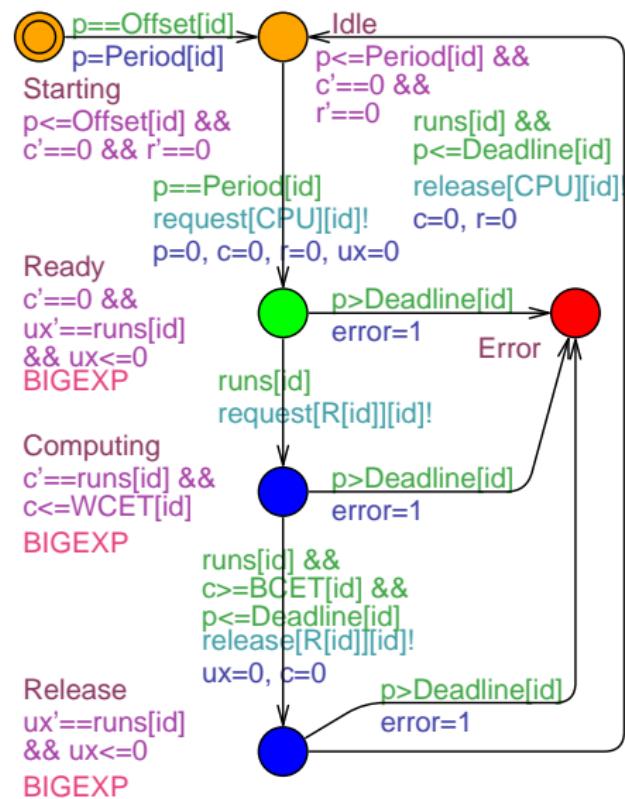
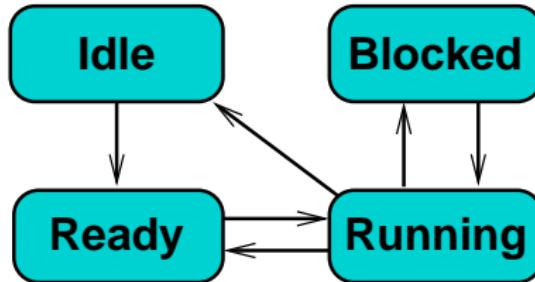
# Template for Task using 1 Resource

## Parameters:

```

1 int Period[task_t]    = { 100, 100, 100 };
2 int Offset[task_t]    = { 20,   0,   10 };
3 int WCET[task_t]      = { 15,  25,  40 };
4 int BCET[task_t]      = { 12,  20,  32 };
5 int Deadline[task_t]  = { 20,  40,  70 };
6 res_t R[task_t]        = { 1,   1,   1 };
7 bool runs[task_t]     = { 0,   0,   0 };
8 bool error = false; // global variable
  
```

## OS task states:



# Satellite Software Task Operations

## Primary Functions

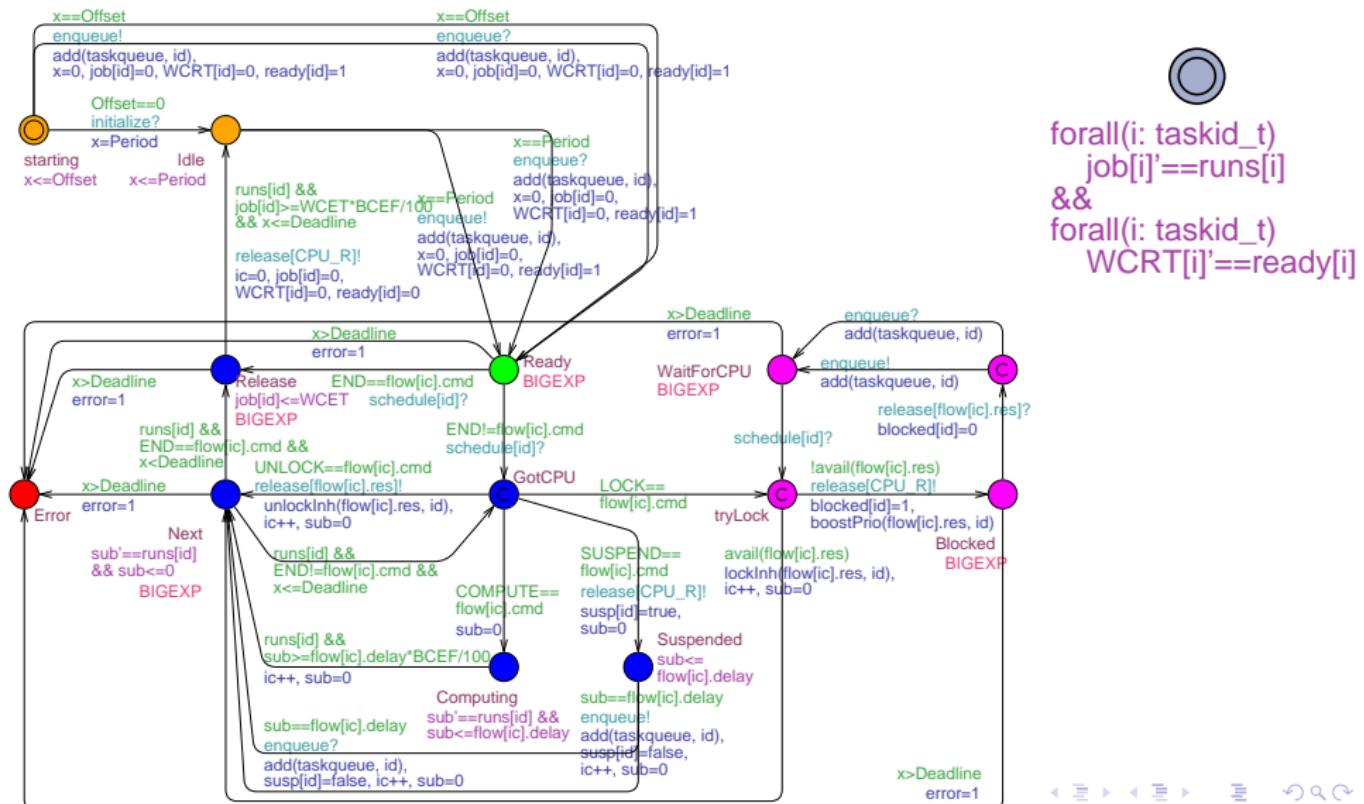
- Data processing	<b>20577</b> /2521 <b>Icb_R</b> (LNS: 2, LCS: <b>1200</b> , LC: <b>1600</b> , MaxLC: 800)
- Guidance	<b>3440</b> /0
- Attitude determination	<b>3751</b> /1777 <b>Sgm_R</b> (LNS: 5, LCS: <b>121</b> , LC: <b>1218</b> , MaxLC: 236)
- PerformExtraChecks	<b>42</b> /0
- SCM controller	<b>3479</b> /2096 <b>PmReq_R</b> (LNS: 4, LCS: <b>1650</b> , LC: <b>3300</b> , MaxLC: 3300)
- Command RWL	<b>2752</b> /85

```
1  typedef int [0,4] funtype_t; // function type
2  const funtype_t END = 0, COMPUTE = 1, // possible functions
   LOCK = 2, UNLOCK = 3, SUSPEND = 4;
3
4  typedef struct {
5      funtype_t cmd; // call function command
6      resid_t res; // resource argument
7      time_t delay; // time argument
8  } fun_t;
9
typedef fun_t ASWFlow_t[28]; // list of functions
```

# Refined Task Operations

```
1 const ASWFlow_t PF_f = { // Primary Functions:  
2     { LOCK,    lcb_R, 0 },           // 0) ----- Data processing  
3     { COMPUTE, CPU_R, 1600–1200 }, // 1) computing with lcb_R  
4     { SUSPEND, CPU_R, 1200 },     // 2) suspended with lcb_R  
5     { UNLOCK, lcb_R, 0 },         // 3)  
6     { COMPUTE, CPU_R, 20577–(1600–1200) }, // 4) computing w/o lcb_R  
7     { COMPUTE, CPU_R, 3440 },      // 5) ----- Guidance  
8     { LOCK,    Sgm_R, 0 },         // 6) ----- Attitude determination  
9     { COMPUTE, CPU_R, 1218–121 }, // 7) computing with Sgm_R  
10    { SUSPEND, CPU_R, 121 },     // 8) suspended with Sgm_R  
11    { UNLOCK, Sgm_R, 0 },        // 9)  
12    { COMPUTE, CPU_R, 3751–(1218–121) }, // 10) computing w/o Sgm_R  
13    { COMPUTE, CPU_R, 42 },       // 11) ----- Perform extra checks  
14    { LOCK,    PmReq_R, 0 },      // 12) ----- SCM controller  
15    { COMPUTE, CPU_R, 3300–1650 }, // 13) computing with PmReq_R  
16    { SUSPEND, CPU_R, 1650 },    // 14) suspended with PmReq_R  
17    { UNLOCK, PmReq_R, 0 },      // 15)  
18    { COMPUTE, CPU_R, 3479–(3300–1650) }, // 16) comp. w/o PmReq_R  
19    { COMPUTE, CPU_R, 2752 },     // 17) ----- Command RWL  
20    { END,    CPU_R, 0 }          // 18) finished  
21};
```

# Template for Satellite Software Task



# Symbolic Verification

- Schedulability:  $A[] \text{ not error}$
- Parameterized model:  $BCET = f \cdot WCET, f \in [0, 1]$

limit cycle	$f = 100\%$			$f = 95\%$		
	states	mem	time	states	mem	time
1	0.001	51.2	1.47	0.5	83.0	15:03
2	0.003	53.7	2.45	0.8	96.8	27:00
4	0.005	54.5	4.62	1.5	97.2	48:02
8	0.010	54.7	8.48	2.8	97.8	1:28:45
16	0.020	55.3	16.11	5.4	112.0	2:45:52
$\infty$	0.196	58.8	2:39.64	52.7	553.9	27:05:07

limit cycle	$f = 90\%$			$f = 86\%$		
	states	mem	time	states	mem	time
1	1.5	124.1	1:22:43	3.3	186.9	6:39:47
2	2.4	139.7	2:09:15	5.3	198.7	9:14:59
4	4.4	138.3	3:48:40	9.2	274.6	14:12:57
8	9.1	156.5	8:38:42	18.2	364.6	28:35:32
16	17.8	176.0	16:42:05	35.4	520.4	44:06:57
$\infty$	181.9	1682.2	147:23:25	<b>pos.unsafe</b>		

# Worst Case Response Times

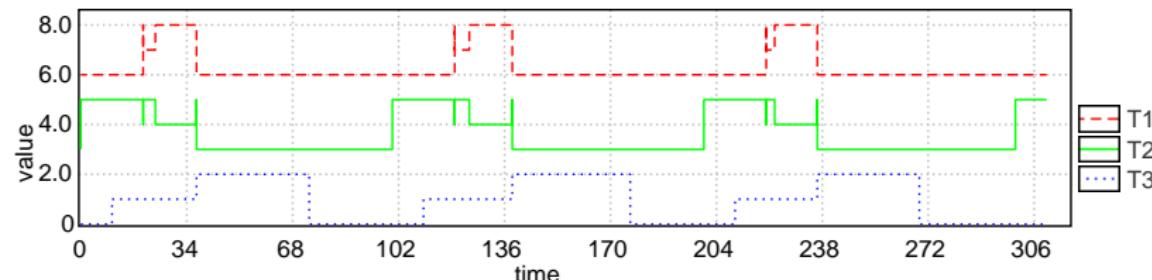
Estimate WCRT: sup: WCRT[1],WCRT[2],...,WCRT[33]

ID	Task	Specification			WCRT			
		Period	WCET	Deadline	Terma	f = 100%	f = 95%	f = 90%
1	RTEMS_RTC	10.000	0.013	1.000	0.050	0.013	0.013	0.013
2	AswSync_SyncPulseslr	250.000	0.070	1.000	0.120	0.083	0.083	0.083
3	Hk_Samplerlsr	125.000	0.070	1.000	0.120	0.070	0.070	0.070
4	SwCyc_CycStartlsr	250.000	0.200	1.000	0.320	0.103	0.103	0.103
5	SwCyc_CycEndlsr	250.000	0.100	1.000	0.220	0.113	0.113	0.113
6	Rt1553_lsr	15.625	0.070	1.000	0.290	0.173	0.173	0.173
7	Bc1553_lsr	20.000	0.070	1.000	0.360	0.243	0.243	0.243
8	Spw_lsr	39.000	0.070	2.000	0.430	0.313	0.313	0.313
9	Obdh_lsr	250.000	0.070	2.000	0.500	0.383	0.383	0.383
10	RtSdb_P_1	15.625	0.150	15.625	4.330	0.533	0.533	0.533
11	RtSdb_P_2	125.000	0.400	15.625	4.870	0.933	0.933	0.933
12	RtSdb_P_3	250.000	0.170	15.625	5.110	1.103	1.103	1.103
13	(no task, this ID is reserved for priority ceiling)							
14	<b>FdirEvents</b>	250.000	5.000	230.220	7.180	5.553	5.553	5.553
15	<b>NominalEvents_1</b>	250.000	0.720	230.220	7.900	6.273	6.273	6.273
16	<b>MainCycle</b>	250.000	0.400	230.220	8.370	6.273	6.273	6.273
17	HkSampler_P_2	125.000	0.500	62.500	11.960	5.380	7.350	8.153
18	HkSampler_P_1	250.000	6.000	62.500	18.460	11.615	13.653	14.153
19	Acb_P	250.000	6.000	50.000	24.680	6.473	6.473	6.473
20	IoCyc_P	250.000	3.000	50.000	27.820	9.473	9.473	9.473
21	<b>PrimaryF</b>	250.000	34.050	<b>59.600</b>	<b>65.47</b>	<b>54.115</b>	<b>56.382</b>	<b>58.586</b>
22	<b>RCSControlF</b>	250.000	4.070	239.600	76.040	53.994	56.943	58.095
23	Obt_P	1000.000	1.100	100.000	74.720	2.503	2.513	2.523
24	Hk_P	250.000	2.750	250.000	6.800	4.953	4.963	4.973
25	StsMon_P	250.000	3.300	125.000	85.050	17.863	27.935	28.086
26	TmGen_P	250.000	4.860	250.000	77.650	9.813	9.823	9.833
27	Sam_P	250.000	4.020	250.000	18.680	14.796	14.880	14.973

# Simulation (small model)

Simulate and inspect a random run (e.g.  $f = 80\%$ ):

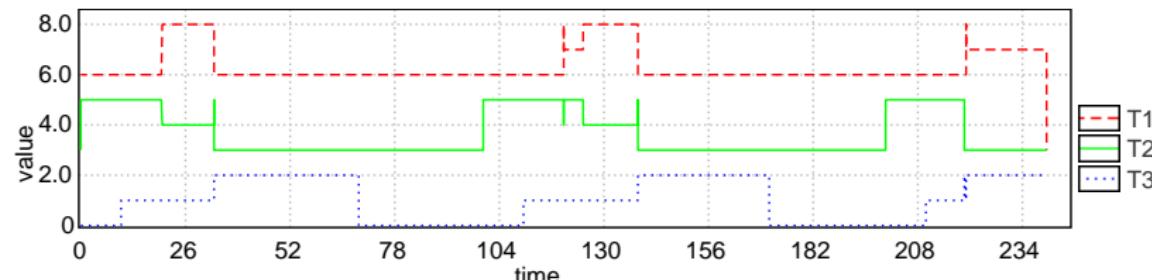
```
simulate 1 [≤300] {
    (T(1).Ready+T(1).Computing+T(1).Release+runs[1]-2*T(1)
     (T(2).Ready+T(2).Computing+T(2).Release+runs[2]-2*T(1)
     (T(3).Ready+T(3).Computing+T(3).Release+runs[3]-2*T(1)
}
```



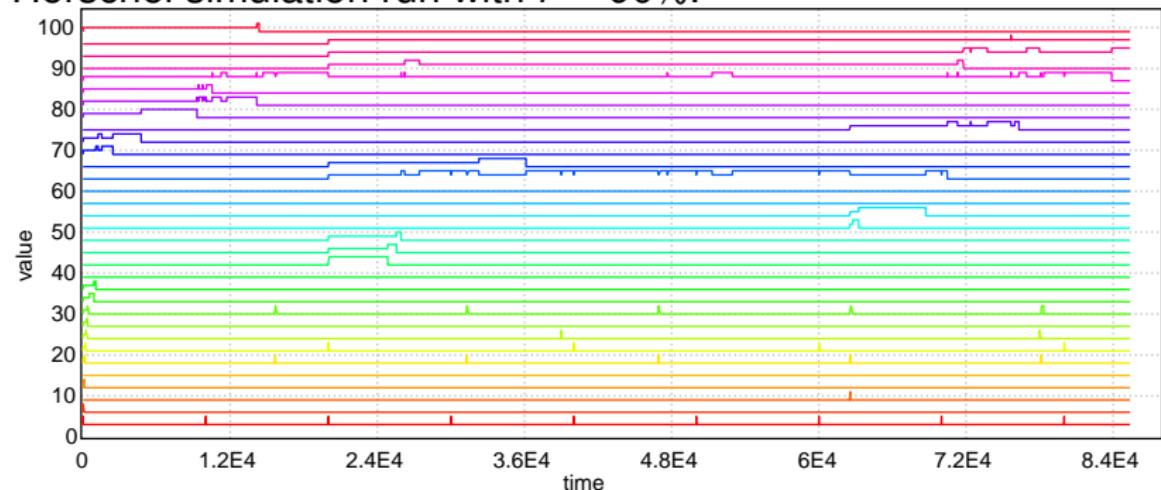
# Simulation (small model)

Find and inspect failing run (e.g.  $f = 79\%$ ):

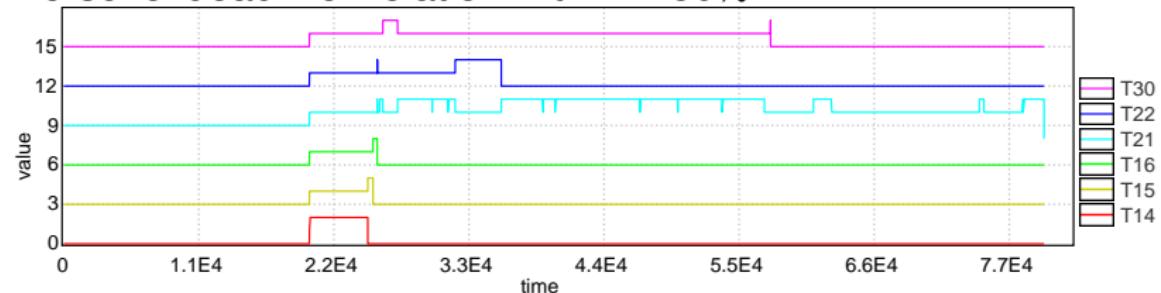
```
simulate 10000 [≤300] {
    (T(1).Ready+T(1).Computing+T(1).Release+runs[1]-2*T(1)
    (T(2).Ready+T(2).Computing+T(2).Release+runs[2]-2*T(1)
    (T(3).Ready+T(3).Computing+T(3).Release+runs[3]-2*T(1)
} : 1 : error
```



## Herschel simulation run with $f = 90\%$ :



## Herschel deadline violation with $f = 50\%$ :



# SMC of Herschel Model

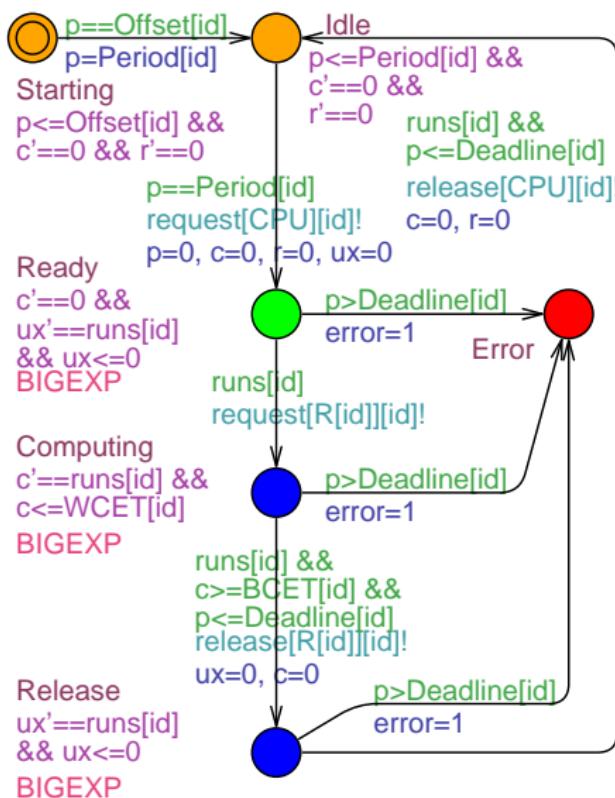
Estimate:  $\Pr[<=\text{LIMIT}*250000](\text{error})$

Limit cycles	f %	SMC parameters $\alpha$	$\varepsilon$	Total traces, #	Error traces #	Probability	Earliest cycle	Error offset	Verification time
1	0	0.0100	0.005	105967	1928	0.018194	0	79600.0	1:58:06
1	50	0.0100	0.005	105967	753	0.007106	0	79600.0	2:00:52
1	60	0.0100	0.005	105967	13	0.000123	0	79778.3	2:01:18
1	62	0.0005	0.002	1036757	34	0.000033	0	79616.4	19:52:22
160	63	0.0100	0.05	1060	177	0.166981	0	81531.6	2:47:03
160	64	0.0100	0.05	1060	118	0.111321	1	79803.0	2:55:13
160	65	0.0500	0.05	738	57	0.077236	3	79648.0	2:06:55
160	66	0.0100	0.05	1060	60	0.056604	2	82504.0	2:62:44
160	67	0.0100	0.05	1060	26	0.024528	1	79789.0	2:64:20
160	68	0.0100	0.05	1060	3	0.002830	67	81000.0	2:67:08
640	69	0.0100	0.05	1060	8	0.007547	114	80000.0	12:23:00
640	70	0.0100	0.05	1060	3	0.002830	6	88070.0	12:30:49
1280	71	0.0100	0.05	1060	2	0.001887	458	80000.0	25:19:35

Just find:

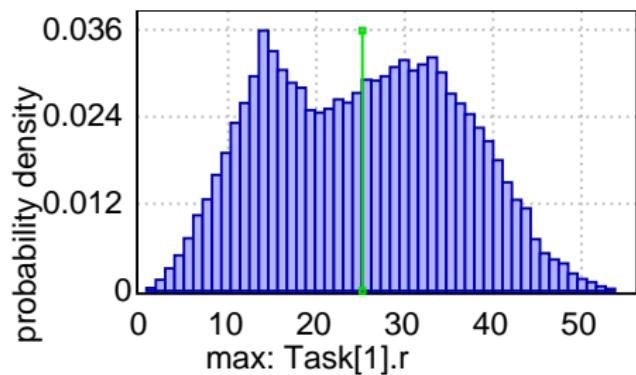
**simulate 10000 [ $<=\text{LIMIT}*250000$ ] { error } :1:error**

# Estimating Response Times using SMC



$$\mathbb{E}[<=200; 50000] \text{ (max: } r)$$

$$\Pr[r \leq 10000] (\neg \text{time} == 200)$$



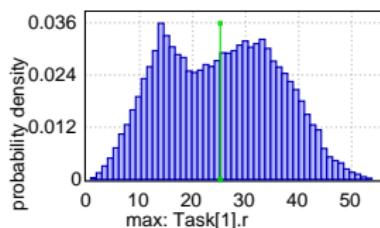
## SMC: Response Times (small model, f=0%)

With  $f = 0\%$  (BCET=0), T1 violates deadline at 20, thus we relax deadline parameters just to inspect the distribution of WCRT.

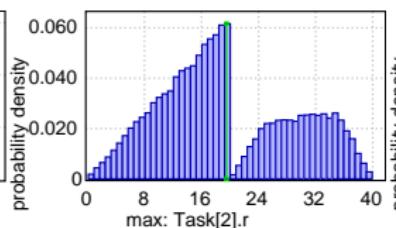
$E[<=200; 50000] \text{ (max: } T(1).r)$

$E[<=200; 50000] \text{ (max: } T(2).r)$

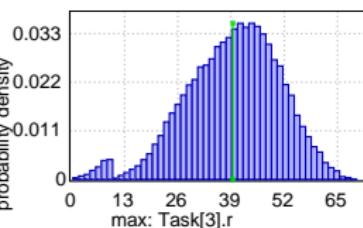
$E[<=200; 50000] \text{ (max: } T(3).r)$



(a) Task T1.



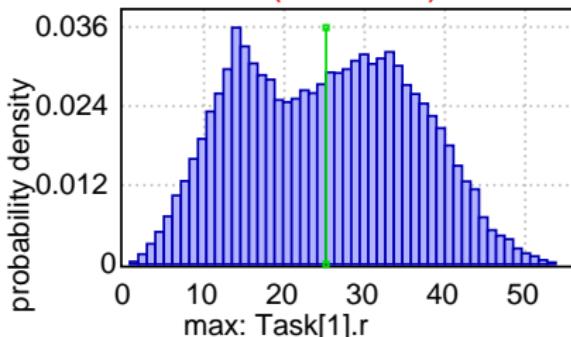
(b) Task T2.



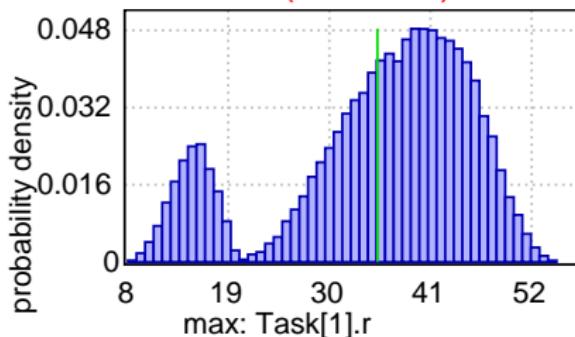
(c) Task T3.

# SMC: Response Times of T1

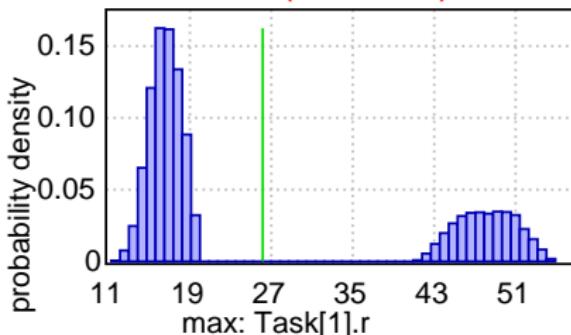
$f = 0\% \text{ (not safe).}$



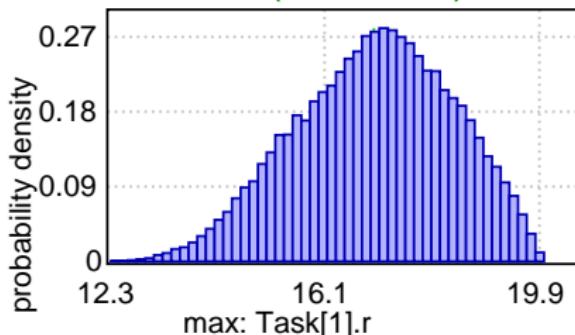
$f = 50\% \text{ (not safe).}$



$f = 79\% \text{ (not safe).}$

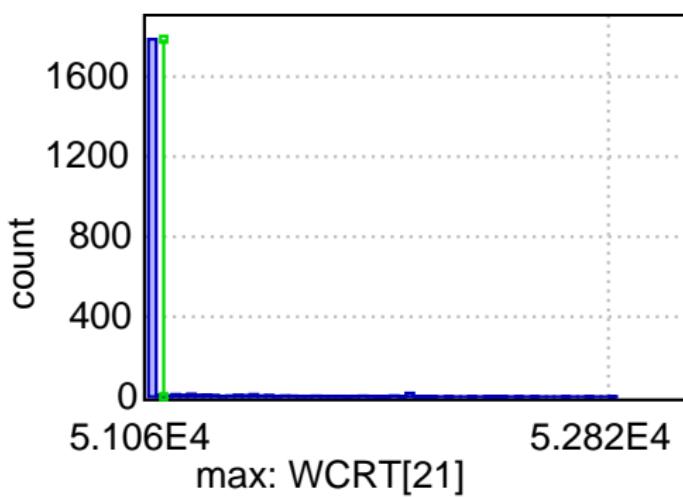


$f = 80\% \text{ (seem OK).}$



# Estimating WCRT for Herschel

E [ $\leq \text{LIMIT} * 250000$ ; 2000] (max: WCRT[21])



Plot for  $f = \text{BCET}/\text{WCET} = 90\%$

# Summary of Techniques Used

- Modeling:
  - Timed automata with clocks to express time constraints.
  - Stop-watches to track task progress.
  - Functions to implement resource sharing protocols.
  - Data structures to specify sequences of task operations.
- Symbolic model checking:
  - Exhaustive exploration of entire model state space.
  - Verification memory saving via sweep-line & CDS.
  - WCRT estimation using supremum query.
- Statistical model checking:
  - Trace visualization via simulate query.
  - Bounded simulations for disproving schedulability
  - WCRT estimation via probability density over clock values.

Thank You  
for your attention